Tuning Shims for High Field Quality in Superconducting Magnets*

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Abstract—A high field quality in quadrupoles for the interaction region is crucial to the luminosity performance of high energy colliders such as the Relativistic Heavy Ion Collider (RHIC). The field quality in magnets is limited in part by manufacturing tolerances in the parts and assembly. A tuning shim method has been developed to reduce the relative field errors ($\Delta B/B$) from $\sim10^{-4}$ to $\sim10^{-5}$ at 2/3 of the coil radius. Eight tuning shims having a variable thickness of iron are inserted after the construction and measurement of field harmonics in the magnet. In this paper the tuning shim technique is described for RHIC interaction region quadrupoles. The results of calculations and measurement are also presented.

I. INTRODUCTION

The Relativistic Heavy Ion Collider [1], [2] being built at Brookhaven National Laboratory (BNL) has six interaction regions. Each interaction region uses twelve 130 mm aperture quadrupoles [3] in four focusing triplets. In order to achieve a high luminosity, the beam will be squeezed to the smallest possible size ($\beta^* = 1$ meter) in two interaction regions. An unavoidable consequence of this is a large increase in beam size in the interaction region quadrupoles. The aperture of these magnets should increase in proportion to the beam size to maintain the nominal field quality for the particle beam. This, however, is not practical for various reasons. As a result, the beam occupies a larger fraction of the aperture in these magnets. In RHIC, the ratio of beam size in these interaction region quadrupoles to the main ring 80 mm aperture quadrupoles is about seven whereas the ratio of coil apertures between the two is about 1.6. Therefore, these quadrupoles strongly influence the beam life time during the high luminosity operation [4]. Moreover, a rapid change in beam size and phase advance within the focusing triplet for the interaction region limits the effectiveness of the correctors [4]. The tuning shim method described in this paper compensates for the field errors right at the source, i.e. in the aperture of these magnets. This compensation has a small current dependence due to iron saturation. The harmonics are minimized at 5 kA (47.7 T/m) operation to maximize the luminosity at the top energy of the machine.

II. FIELD HARMONICS IN SUPERCONDUCTING MAGNETS

The skew ($a_n$) and normal ($b_n$) components of field harmonics are defined as follows:

$$B_y + iB_x = 10^{-4} G \times R \sum_{n=0}^{\infty} \left[ b_n + i a_n \right] \frac{x + iy}{R^n} ,$$

where $B_x$ and $B_y$ are the components of the field at $(x,y)$, $G$ is the gradient at the center of the quadrupole and $R$ is the reference radius, which is 40 mm in these magnets.

In a perfect quadrupole magnet, all harmonics except the fundamental one ($b_1 = 10^4$) are zero. A non-zero value of the other harmonics may be due to (a) design deficiency from the limited number of parameters available in cross section optimization, (b) mechanical errors from the practical tolerances in the parts used in building magnets, and (c) errors or non-reproducibility in the manufacturing process. To get the harmonics better than a few units (or field errors better than $10^{-4}$), the cumulative deviation from the ideal geometry should be less than 0.05 mm. This is at the limit of what can be practically achieved.

III. MAGNET DESIGN

The magnetic length of the three interaction region quadrupoles in the focusing triplet are 1.44 m, 3.4 m and 2.1 m. They all have the same cross section. The detailed design of these magnets is described elsewhere [3].

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Fig. 1. Cross section of the 130 mm aperture RHIC interaction region quadrupoles. 1A, 1B, etc. are the locations of eight gaps for tuning shims.
A. Cross Section Design of the Magnet

The cross section of these magnets is shown in Fig. 1. The design is based on a single layer coil geometry where the iron yoke also acts as a collar to provide the necessary pre-compression on the coils. The yoke inner surface consists of two circular radii instead of the usual one radius to reduce the saturation induced \( b_5 \). The yoke inner radius is 87 mm at the midplane and 92 mm at the pole. The space between the coil and yoke is filled with a thin, glass-filled, phenolic spacer. The outer surface of the spacer also has two radii, 87 mm at the midplane and 92 mm at the pole. However, eight gaps are left between the yoke and phenolic spacer. The location of gap 2B in the first octant is about 30° (see Fig. 1). The location of the other seven gaps is determined by the quadrupole symmetry, for example gap 2A is at 60°, 1B is at 120°, etc.

B. Mechanical Design of the Tuning Shims

A schematic diagram of the tuning shim in the magnet at location 1B is shown in Fig. 2. The actual tuning shim is a package of a number of low carbon steel (magnetic) and brass (non-magnetic) laminations. The use of laminated iron assures small eddy currents. These laminations have a width of 6.6 mm and a thickness of either 0.125 mm or 0.5 mm. The total thickness of all laminations in each tuning shim package is always 6.1 mm, but the proportion of iron laminations varies. The lamination pack is cured into a parallelogram shape in a fixture with epoxy between the laminations. At the end of the curing cycle the tuning shim package is quite sturdy and can be handled easily. The width of the lamination pack is 7.5 mm and the thickness is 6.35 mm. The above size provides a small but sufficient clearance for easy insertion of tuning shims into the magnet. The two thicknesses of laminations (0.125 mm and 0.5 mm) provide the necessary resolution in the harmonic correction while keeping the number of laminations to a reasonable value. The nominal magnetic thickness of the tuning shim is 3.175 mm, of which 3.05 mm is occupied by the iron laminations. The presence of epoxy reduces the iron packing factor by ~4%.

The tuning shims are placed such that the iron laminations are next to the yoke to provide a better magnetic circuit. A 0.1 mm thick sheet is used between the tuning shim and yoke to provide insulation against eddy currents.

IV. THEORY AND CALCULATIONS FOR TUNING SHIMS

A. Basic Principle

To compensate the error harmonics in the magnet, an iron shim can be attached to the inner surface of the yoke (see, for example, [5]). This gets magnetized and distorts the field in the magnet aperture. We express this distortion in terms of field harmonics. The harmonics created by these shims are used to cancel out the previously measured harmonics in the magnet. In general, a properly chosen location of “n” shims, can compensate up to “n” harmonics. However, these “n” harmonics can not be “n” arbitrary harmonics. The symmetry and the angular location of the shims determine which harmonics will change. These shims are called tuning shims because the amount of iron in each shim is tuned according to the harmonics measured in each magnet so that the corrected harmonics are minimized.

B. Independent and Coupled Changes in Harmonics

A consequence of correcting field harmonics with tuning shims is the creation of other harmonics in the process. These other harmonics are those that are allowed by the symmetry of the shims.

In this design, eight tuning shims correct eight harmonics. However, the following three rules apply: (1) of eight harmonics, four must be skew \( a_n \) and four must be normal \( b_n \), (2) of the four skew and four normal harmonics, two must be odd (e.g. \( a_3 \)) and two must be even (e.g. \( b_4 \)), and finally (3) for any change in an odd harmonic \( n=2k+1 \), the harmonic \( n=2k+5 \) will also change, e.g. a change in \( b_3 \) will cause a coupled change in \( b_7 \), as well. Despite the above restrictions, the desired eight harmonics \( (a_2, a_3, a_4, a_5) \) and \( (b_2, b_3, b_4, b_5) \) can be independently minimized. Having chosen the change in these harmonics, the change in the other harmonics is determined by the coupling. However, their values can be minimized by properly choosing the shim locations.

C. Calculations for Low Field Correction

At low field the permeability of iron is large and the change in harmonics created by tuning shims is independent of the field. The computed changes (as compared to the “no shim” or the “zero iron thickness” case) in skew \( a_n \) and normal
harmonics ($b_n$) created by a 4 mm thick tuning shim at low current, are given in Table I. Whereas, the change in the magnitude and sign of allowed harmonics (transfer function, $b_3$, $b_5$, etc.), is independent of the shim location, the change in other harmonics depends on the location - at four locations the change has a positive sign and at the other four a negative sign. The computer code POISSON [6] was used for carrying out these calculations.

### C. Calculations for High Fields Correction

At high field the relative change in magnetization is not proportional to field and as a result the change in harmonics produced by tuning shims becomes current dependent. In Table II, we examine the loss in harmonic correction due to iron saturation. These calculations are performed for the harmonics created by the nominal size (3.175 mm) tuning shim. In Table II, the results of calculations are given for one of several shim locations that gives the maximum change in that harmonic. The change in harmonics due to a 4 mm thick tuning shim (as compared to the no shim case) at various locations at low current. The computer code POISSON [6] was used for carrying these calculations.

#### Table I

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#### V. COMPARISON WITH MEASUREMENTS

The validity of tuning shim method and model calculations has been investigated with a number of measurements. An exhaustive series of measurements have been done at room temperature (warm measurements) when a small current is carried by the copper in the cable. These measurements could be done much faster and although they do not reflect the true operating conditions, they nevertheless provide good verification for the harmonics created by a change in geometry. A limited number of measurements have also been performed (cold) at the design operating current (5kA). In this section, a comparison between the calculations and measurements is presented.

**A. Warm Measurements**

During the warm measurements, we inserted tuning shims having thickness of 1.5875 mm, 3.175 mm (nominal) and 4.7625 mm. The measurements were performed after inserting/changing a tuning shim in each of the eight locations to obtain the change from the “no shim” or “zero iron thickness” case. In Fig. 3, we show the measured change in harmonics for the given size tuning shim using 8 types of symbols for eight locations and the computed change by 8 types of lines. Good agreement between the calculations and measurements is apparent.

**B. Cold Measurements**

In Table III, we compare magnetic measurements at 5 kA with calculations when the thickness of the tuning shim in locations 1A, 2B, 3A, 4B was 2.91 mm and at other four locations was 3.44 mm. This configuration creates only odd $b_n$ harmonics; others are not expected from symmetry. The measured values of such unexpected harmonics was within the measurement errors. A relatively large error in calculations is expected at 5kA due to the complexity of the computer model and uncertainty in the magnetic properties of the lamination stack used.
Fig. 3. A comparison between calculations and warm measurements for the field harmonics created by tuning shims. These are the changes in harmonics relative to the “no shim” or “zero iron thickness” case for each shim. The eight symbols represent the measurements for the eight tuning shim locations and eight lines are the calculations for these locations.
VI. PROCEDURE FOR HARMONIC CORRECTION WITH TUNING SHIMS IN RHIC INSERTION QUADRUPOLES

The tuning shims will be installed inside the magnet without opening it. This makes the process more efficient since de-assembling and re-assembling of the magnet takes a long time and has a potential for damaging the magnet. Moreover, at the $10^{-5}$ level, the harmonics may change during re-assembly, since the exact location of the conductors may not be reproducible during each magnet assembly.

The harmonic correction will be applied on the basis of warm measurements. This assumes that a good warm to cold correlation for the harmonics in the magnets and for the change produced by tuning shims is obtained prior to implementing this procedure. The thickness of eight tuning shims for each magnet would be computed to minimize the eight harmonics. The systematic values of field harmonics which are allowed by the magnet geometry, have been already minimized [7] so that a large tuning shim correction is not required. A second set of warm magnetic measurement will be performed to confirm the correct installation of the tuning shims. Finally, the harmonics will be measured cold at 5 kA, where they should be ideally zero. In principle, if the tuning shim correction is not satisfactory in this attempt, one can make a small iteration in tuning shim sizes to make the desired harmonics zero within the measurement errors.

VII. DISCUSSION

A special situation arose in correcting the normal octupole ($b_3$) harmonic in these magnets. This is a non-allowed harmonic in an ideal quadrupole geometry. However, for economic reasons, these quadrupoles are collared in a dipole press. The collaring process distorts the coil geometry such that a large $b_3$ (~7 units) is generated. If this is corrected by the tuning shim method alone, a large $b_7$ will be created. However, $b_3$ can also be corrected with an asymmetric coil to midplane gap between the horizontal and vertical planes [7]. This generates a $b_7$ that is of opposite sign to that generated in the tuning shim method. We have used a combination of the two methods to minimize both $b_3$ and $b_7$ harmonics.

The coil pole shims and coil midplane shims were adjusted during the magnet production to keep the values of allowed harmonics $b_5$ and $b_9$ low, so that a large tuning shim correction is not required.

A computer program SHIMCAL [8] has been written to compute the thickness of eight shims for compensating eight measured harmonics at 5 kA. At present it uses numerically computed coefficients based on POISSON calculations. Due to a large iron saturation at 5 kA and due to complexity of the problem, analytic formulae cannot be derived. Thus after a series of magnetic measurements at 5 kA, experimentally determined coefficients will be used in the program.

VIII. CONCLUSIONS

The field quality in superconducting magnets can be improved from the present $10^{-4}$ level to the $10^{-5}$ level using the tuning shim method described in this paper. Good agreement between the calculations and warm measurements as well as cold measurements proves the effectiveness of the concept. The use of the tuning shim method could also relieve the tolerances in parts and manufacturing of the magnets. However, a large correction in lower order harmonics could generate significant values of higher order harmonics.

ACKNOWLEDGMENT

M. Harrison’s appreciation for the usefulness of the tuning shim method for the high luminosity collider was critical to the development of this program. Ongoing discussions with S. Peggs and J. Wei regarding the beam dynamics issues was the guide for improving field quality in the RHIC interaction region quadrupoles.

REFERENCES